

PROTEIN – LIGAND BINDING

(Precaution to be taken to avoid the occurrence of wrong result)

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ABSTRACT

The dissociation of a protein – ligand complex (PL) can be described by a simple equilibrium reaction $PL \rightleftharpoons P + L$ the corresponding equilibrium relationship is defined $K [PL] = [P] [L]$ (K = dissociation constant) In this equation $[P] = [P]_T - [PL]$ and $[L] = [L]_T - [PL]$ where $[P]_T$ and $[L]_T$ are the initial total concentrations of the protein and ligand, respectively. **Case1:** If we substitute $[L]_T - [PL]$ for $[L]$ and $[P]_T - [PL]$ for $[P]$, then equilibrium relationship becomes $K [PL] = ([L]_T - [PL]) ([P]_T - [PL])$ From this it follows that $[PL] = [L]_T [P] / K + [P]$ **Case2:** If we substitute $[L]_T - [PL]$ for $[L]$, $[P]_T - [PL]$ for $[P]$ and $[P]_T - [P]$ for $[PL]$, then equilibrium relationship becomes $K ([P]_T - [P]) = ([L]_T - [PL]) ([P]_T - [PL])$ From this it follows that $K - [L] = K F_{FP} - F_{BP} [L]$ (wrong result) **Conclusion:** Substitution for '[PL]' along with the substitutions for '[L]' and '[P]' should be avoided in order to prevent the occurrence of wrong result.

KEYWORDS

Protein –ligand binding, protein - ligand complex, equilibrium reaction, dissociation constant.

CASE 1

Using the equilibrium relationship

$K [PL] = [L] [P]$ and substituting,

$[L]_T - [PL]$ for $[L]$

$[P]_T - [PL]$ for $[P]$

Gives:

$$K [PL] = \{[L]_T - [PL]\} \{[P]_T - [PL]\}$$

$$= [L]_T [P]_T - [PL] [L]_T - [PL] [P]_T + [PL]^2$$

Dividing throughout by $[PL]$ gives:

$$K = \{[L]_T [P]_T / [PL]\} - [L]_T - [P]_T + [PL]$$

But

$$[P]_T = [PL] + [P]$$

And, therefore,

$$K = \{[L]_T [P]_T / [PL]\} - [L]_T - [P]$$

$$= [L]_T \{([P]_T / [PL]) - 1\} - [P]$$

From this it follows that

$$K + [P] = [L]_T [P] / [PL]$$

Rearranging

$$[PL] = [L]_T [P] / K + [P] \quad (1)$$

DISCUSSION

This defines a rectangular hyperbola with several important regional properties:

1. Saturation: when $[P] \gg K$, $[PL]$ asymptotically approaches $[L]_T$.
2. Half-saturation: when $[P] = K$, $[PL] = [L]_T / 2$ - in other word, the dissociation constant is equal to the (free) protein concentration needed to ensure that 50% of the ligand will be bounded.
3. Linearity: when $[P] \ll K$, $[PL]$ is $\sim$ proportional to $[P]$ with slope $= [L]_T / K$.

CASE 2

Using the equilibrium relationship

$K [PL] = [L] [P]$ and substituting,

$[P]_T - [P]$ for $[PL]$ $[L]_T - [PL]$ for $[L]$

$[P]_T - [PL]$ for $[P]$

Gives:

$$K \{[P]_T - [P]\} = \{[L]_T - [PL]\} \{[P]_T - [PL]\}$$

$$K [P]_T - K [P] = [L]_T [P]_T - [PL] [L]_T - [PL] [P]_T + [PL]^2$$

Rearranging

$$K [P]_T - [L]_T [P]_T + [PL] [P]_T = - [PL] [L]_T + [PL]^2 + K [P]$$

$$[P]_T \{K - [L]_T + [PL]\} = [PL] \{-[L]_T + [PL]\} + K [P]$$

Further, if we substitute

$$[L]_T = [PL] + [L]$$

Then we get

$$[P]_T \{K - [PL] - [L] + [PL]\} = [PL] \{-[PL] - [L] + [PL]\} + K [P]$$

$$[P]_T \{K - [L]\} = - [PL] [L] + K [P]$$

Which is the same as:

$$[P]_T \{K - [L]\} = K [P] - [PL] [L]$$

$$K - [L] = K \{[P] / [P]_T\} - \{[PL] / [P]_T\} [L]$$

Labeling

$[P] / [P]_T$ as F_{FP} (fraction of free protein) and $[PL] / [P]_T$ as F_{BP} (fraction of bound protein) then above expression turn into

$$K - [L] = K F_{FP} - F_{BP} [L] \quad (2)$$

DISCUSSION

1. If $F_{FP} = F_{BP}=1$, then the LHS = RHS, and the Eq. (2) is true.
2. If $F_{FP} = F_{BP} \neq 1$, then the LHS $\neq$ RHS, and the Eq. (2) is invalid.

Let us now check the validity of the condition " $F_{FP} = F_{BP}=1$ ".

As per the protein conservation law,

$$[P]_T = [PL] + [P]$$

From this it follows that

$$1 = F_{BP} + F_{FP}$$

If we assume $F_{BP} = F_{FP}=1$, we get:

$$1 = 2$$

The condition $F_{FP} = F_{BP} = 1$ is invalid, since $1 \neq 2$.

In fact, the only way it can happen that $K - [L] = K - [L]$ is if both $F_{FP} = F_{BP}=1$. Since $F_{FP} = F_{BP} \neq 1$, Eq. (2) does not therefore hold well.

CASE NOTES

CASE 1

If we substitute $[L]_T - [PL]$ for $[L]$ and $[P]_T - [PL]$ for $[P]$, then equilibrium relationship $K [PL] = [L] [P]$ becomes

$$K [PL] = ([L]_T - [PL]) ([P]_T - [PL])$$

From this it follows that

$$[PL] = [L]_T [P] / K + [P]$$

CASE 2

If we substitute $[L]_T - [PL]$ for $[L]$, $[P]_T - [PL]$ for $[P]$ and $[P]_T - [P]$ for $[PL]$, then equilibrium relationship $K [PL] = [L] [P]$ becomes

$$K ([P]_T - [P]) = ([L]_T - [PL]) ([P]_T - [PL])$$

From this it follows that

$$K - [L] = K F_{FP} - F_{BP} [L] \quad (\text{wrong result})$$

CONCLUSION

Substitution for '[PL]' along with the substitutions for '[L]' and '[P]' should be avoided in order to prevent the occurrence of wrong result.

REFERENCES

1. Binding D B by Michael K. Gilson, pharmacy.ucsd.edu/labs/Gilson/BindingDB-Intro.pdf (2009).
2. Biochemistry by Reginald H. Garrett and Charles M. Grisham (chapter 5), © 2010 by Brooks/Cole, Cengage Learning Inc.
3. Enzymes: Biochemistry Biotechnology Clinical Chemistry by Trevor Palmer (Chapter 12), © 2001 by Horwood Pub Ltd.



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